

WORKSHEET(DIFFERENTIAL CALCULUS)

CLASS XII (OPTIONAL)

1. Verify Lagrange's Mean Value Theorem for the function $f(x) = e^x$ in $[0,1]$
2. Find $\frac{dy}{dx}$ if $x = \frac{\sin^3 t}{\sqrt{\cos 2t}}$ and $y = \frac{\cos^3 t}{\sqrt{\cos 2t}}$
3. If $x^y = e^{x-y}$ prove that $\frac{dy}{dx} = \frac{\log x}{(1+\log x)^2}$
4. Find the second derivative of $e^{x \tan x}$
5. Find the differential coefficient of $\tan x$ by first principle.
6. Verify Rolle's Theorem for $f(x) = \sin x$
7. $= 0$
8. Find $\frac{d^2y}{dx^2}$ if $x = a(\theta + \sin \theta)$, $y = a(1 - \cos \theta)$
9. If $y = a \cos(\log x) + b \sin(\log x)$, $x > 0$ prove that $x^2 y'' + xy' + y = 0$ in $\left[0, \frac{\pi}{2}\right]$
10. If $y = 2\sin x + 3\cos x$.prove that $y + \frac{d^2y}{dx^2} = 0$ prove that $x^2 y'' + xy' + y = 0$
11. If $y = \tan x + \sec x$, prove that $\frac{d^2y}{dx^2} = \frac{\cos x}{(1-\sin x)^2}$
